# Parametrized MTree Clusterer for Weka

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*In the area of clustering, proposing or improving new algorithms represents a challenging task due to an already existing well-established list of algorithms and various implementations that al- low rapid evaluation against tasks on publicly available datasets. In this work, we present an improved version of the MTree clustering algorithm implemented within Weka workbench. The algorithmic approach starts from classical metric spaces and integrates sparametrised business logic for finding the optimal number of clusters, choosing the division policy and other characteristics.* *The result is a versatile data structure that may be used in clustering to find the optimal number of clusters, but mainly for loading data sets that already have a known structure. Experimental results show that MTree finds the proper structure in two clustering tasks, although other algorithms fail in various ways. A discussion of further improvements and experiments on real data sets and functions is included.*

*Povzetek:*

# Introduction

As an unsupervised learning technique, clustering is continuously getting attention within the machine learning area due to many available algorithms and a wide range of application domains for which practical solutions are continually being designed and implemented.

The general problem of building clusters of objects is narrowed down in [41] by clearly stating that the first thing that needs to be taken into consideration in the context of the problem. Therefore, building a general-purpose clustering algorithm that may work with any objects and solve any task is not a realistic option. Thus, the objects we need to define and provide a proper task description accompanied by particular distance and evaluation metrics or various algorithmic approaches need to be carefully taken care of in building a clustering data analysis workflows.

In [1], authors recently raised the problem of clusterability of a dataset. Having an available dataset does not necessarily imply that we may meaningfully run a clustering process to solve a particular task. Thus, defining clusterability becomes a critical issue. Checking if a dataset is clusterable becomes an inherently tricky problem, especially when dealing with actual data and solving a particular practical task.

The wide range of approaches used in available implemented clustering algorithms has found various application domains to provide efficient solutions to many practical tackled problems. From the many application domains, we mention medical im- age processing (i.e., pattern recognition and image segmentation) [39] [24], general and natural language processing knowledge discovery [20] [33] [34], navigation of robots [14] [22] and in many other contexts.

In the area of unsupervised learning, there are several general classes of clustering algorithms (i.e., flat, hierarchical and density-based) that all share two common problems: finding the optimal number of clusters and quickly and efficiently finding the correct clusters taking into consideration specific distance measures appropriate for the objects (i.e., pixels, points, persons, books, etc.) that are being grouped. Further, once the clusters are being correctly determined, there may be later used to query for the nearest neighbours or run specific range queries. Depending upon the inner data structures used for managing the clusters when tree data structures are being used efficiently, searching or traversing may be accomplished efficiently.

The objective of this work is to present an improved version of the metric trees (MTree) algorithm that has been firstly proposed by [7] and later by [40] and [43]. The first proposal of using MTrees in the context of clustering has been made in [31] and later implemented as Weka [16] package in [30]. This paper presents an improved version of the works from [30 and 31] that has been tested in a comparative benchmark with k-MS morphological reconstruction clustering algorithm [37] along with classical algorithms (i.e., simple k-means, Cobweb, Farther First and Canopy) in [9].

This paper presents a further improved sparametrised version of the MTree algorithm in terms of managed items, used distance, the method for finding and setting K (i.e., the number of clusters), division policy and validation metrics. The critical improvement of the new sparametrised version of the MTree clusterer is that it is now suitable to address a broader range of problems. The sparametrised version is not ideal for solving any clustering problem by dynamically choosing the suitable parameters. Instead, a wide range of clustering problems may be addressed to the newly proposed MTree cluster by properly setting its parameters depending on the available data objects and the tackled task.

In general, there are two types of clustering problems. One regards finding patterns in a dataset that we do not know if they have a specific structure or if a certain number of clusters exist. The second type of task regards correctly building a data clustering model that may later be queried many times for getting specific information about managed data. In this scenario, the cluster model is constructed only once such that it may be regarded as a preprocessing step. Later, few insertions and updates may occur at runtime, while most calls are range queries or kNN queries that need to be solved correctly and efficiently. The proposed approach is suited for both tasks, but the second one is more appropriate. Range queries determine items whose distance from a specific query item is smaller than a particular value.

The paper is sorganised as follows. In Section 2, we perform a literature review with regards to similar libraries other application domain usages of metric trees for clustering such as time series analysis of cytometry data, recommender systems, spatial clustering data, automatic computing the number of clusters for colour or greyscale image segmentation and clustering quality metrics. Section 3 describes the proposed approach with a detailed presentation of how each parameter may be set and how it influences the business logic of the MTree. Section 4 presents the experimental results on two publicly available data sets with runs on several parameter settings. Finally, section 5 contains the conclusions of this work, ssummarises the main contributions and discusses potential improvements and applications.

# Related work, limitations and approaches

Data clustering (also known as unsupervised learning) represents a subarea of machine learning. Other areas of machine learning are supervised learning, reinforcement learning or deep learning. A particular sub-domain is represented by age clustering and segmentation [13] which presents the use of subtractive clustering along with classical K-means algorithm to preprocess the data for optimal centroid initialisation. The experimental results were obtained on medical images representing infected blood cells with malaria. The classical images used for segmentation bring better results than k-means taking into account root mean square error (RMSE) and peak signal-to-noise ratio (PSNR) metrics.

Another approach for image clustering was proposed by Chang et al. in [5]. They present a Deep Adaptive Clustering (DAC) approach that reduces to a classification problem in which similarity is determined by cosine distance and learned labelled features tend to be one-hot vectors obtaining good results on popular and accessible datasets like MNIST, CIFAR- 10 and STL-10.

One of the critical practical usages of clustering algorithms is image segmentation. Including spatial information and taking outlier points later in the clustering algorithm has been proposed in [42]. From this perspective, outliers are data points with almost equal distance to their adjacent clusters and should be considered later. This approach raises two issues. One regards the fact that the order in which data points are given to the algorithm is essential. Thus, custom preprocessing may be necessary if a clustering algorithm is highly sensitive to the order in which data points are provided. The second issue regards the very nature of the data set from the clusterability perspective. The critical verification that is also highly recommended is to always check for clusterability before starting the clustering analysis.

Another application of clustering is greyscaling image segmentation [44]. Compared with the clustering of colour images or images that incorporate spatial information, the task is to decrease the algorithm's time complexity by using the affinity propagation (AP) clustering algorithm. As always, when real-life greyscale images are being clustered, the problem of correctly determining the number of clusters or segments is critical.

More elaborate applications regard indexing and retrieval of similar images from an image database (CBIR - Content-Based Image Retrieval), which represent a challenging task that has been addressed in [29] and [27]. The first approach uses features, colour and texture. It employs K-means and hierarchical clustering for finding the most similar images. The second approach uses colour, texture and shape as features and K-means as business logic for determining four classes of images: dinosaurs, flowers, buses and elephants. The obtained experimental results are promising in terms of excellent precision and recall values.

Clustering has also been used successfully in recommender systems that were based on collaborative filtering [11]. A novel K-medoids clustering recommendation algorithm has been proposed, which introduced an improved Kullback-Leibler divergence for computing item similarity. The final task was to improve the effectiveness of the developed recommendation system.

Lately, in the application domain of immunology, clustering algorithms have been used - ChronoClust, a new density-based clustering algorithm - on time series cytometry data [26]. The task was to scharacterise the immune response to disease by tracking temporal evolution.

Recent works [1] emphasised defining clusterability and checking if a dataset is clusterable as a preprocessing step before any other data analysis is further performed. Therefore, a sanity check may be required before applying the algorithm for solving a task that involves clustering. We should verify the clusterability of the dataset. In other words, clustering may not work on data sets that do not show any internal structure, regardless of any specific algorithm employed. In our case, clusterability becomes a prerequisite that the dataset needs to meet before being loaded into the MTree structure. The new proposed clustering algorithm should have as main scenario working with data that is known to be clusterable, for which we know it has a well-defined structure with a known number of clusters. A dataset has a well-defined structure when there exists an assignment of items into clusters that is validated by a domain specialist for real world datasets. In the case of synthetic datasets, the function that creates the instances is designed in such a way that clusters are well-defined and represent the gold labeling for any clustering algorithm.

If the number of clusters is not known, then the results highly depend on the particular practical context of the clustering problem. The context is defined by the problem (clustered objects and clustering task) and parameters of the MTree: object type, distance function, splitting policy and validation metrics. If the data set is not clusterable, we argue that the MTree algorithm and other clustering algorithms will exhibit undefined behaviour.

A more complex context occurs when the image source is unknown or when the ground truth for the training dataset is also unknown [4] [10]. In this particular situation, finding the optimal K represents am an inherently difficult task. From an experimental algorithmic perspective, using proper distance metrics and loss function in this soptimisation problem represents one of the key ingredients towards successful results. Such approaches propose fancy solutions such as hierarchical clustering or clustering ensembles based graph partitioning methods, cluster-based Similarity Partitioning Algorithm (CSPA), HyperGraph Partitioning Algorithm (HGPA), and Meta Clustering Algorithm (MCLA).

Among the most well-known issues in unsupervised learning is determining the actual number of clusters from a data set. Unfortunately, scenarios in which the value of K is known to occur only in a few practical systems. In general, an application that performs an image processing task does not have any information regarding the actual number of clusters from the target image. This situation may occur when dealing with data streams [25] or very high-dimensional data sets [17]. In general, one of the most suitable approaches tries to reduce the automatic determination of K based on dynamic clustering [17] or joint tracking segmentation [32].

A general-purpose algorithm for finding the optimal number of clusters has been proposed by [6] and implemented in an R package in NbClust. The main idea of this approach is that it may use up to 30 indices for voting the number of clusters. The package has implemented a function to run a clustering algorithm (i.e., k-means or hierarchical clustering) using various distance measures and aggregation methods. The main limitation of the approach is that it is general and practical usage for particular datasets that needs to be sparametrised by the appropriate clustering algorithm, subset of indices, distance measure and aggregation method.

One particular usage of clustering regards automatic computing of the number of clusters for colour image segmentation [21]. This approach uses fuzzy c- means algorithms for extracting chromaticity features of colours and trains a Neural-Networks with obtained chromatic data of colours. The trained model may be further used on new colour images to predict the number of clusters in coloured pictures.

Among many clustering libraries, we mention LEAC [36]. It is an open-source library with source code publicly available in the GitHub repository. Thus, once the experiments are also performed on publicly available data sets, the results may be reproducible and used in other setups for further improvements. The inclusion of 23 state-of-the-art Evolutionary Algorithms for partial clustering within a library that allows easy and fast development and integration of a new clustering algorithm represents the solution that we also target when improving the initial version of the MTree clustering algorithm within Weka package.

Another usage of metric trees has been reported recently in [12]. The task is to quickly and efficiently scale up the problem of shadow rendering for 70 million objects (i.e., triangles) in real-time. The proposed metric tree used as splitting policy binary space partitioning (BSP) and ternary object partitioning (TOP) for grouping triangles into clusters as precomputed bounding capsules (line-swept spheres).

Finally, the whole clustering process needs validation, and many quality metrics may accomplish this for a wide range of algorithms [18]. Depending on the structure of the dataset, various clustering quality frameworks [23], [38] have been proposed. The key issue that always arises regards choosing the proper similarity and quality metrics [38].

# Proposed approach

The proposed MTree sparametrised clusterer has been firstly proposed in [31] in an attempt to define a new clustering algorithm that has as main business logic the metric trees initially presented in [7] and later in [40] and [43]. The initial C++ implementation approach was designed to cluster students defined by three of their obtained grades during one semester. The main shortcoming of the proposed structure was that it as designed only for managing student objects and had several hard-coded parameters needed for building the tree. The most important one is *nrKeys*, representing the maximum number of students in a node (i.e., a cluster). This approach has a critical limitation because the *splitNote()* method was called based only when a node was full. Other limitations include the lack of sparametrised division policy, distance metrics, or other features needed to run a clustering process flexibly.

Later, the initially proposed MTree clustering algorithm was contributed as an official Weka package [30]. This newly Java-based approach had the goal to be functionally available under Weka workbench as any other clusterer, such that it may be further used in various practical situations. The MTree clusterer from Weka has been used in [37] in a comparative analysis on publicly available images. The results of MTree were inferior such that the limitations were addressed in [9]. As critical improvements, the MTree version from [9] uses off-line dataset preprocessing for finding the optimal number of clusters and adjusts the business logic of the clusterer in terms of division policy and distance metric between instances. The current proposed version of the MTree cluster represents a flexible sparametrised version of the former in terms of division policy, used distance, the method for finding and setting the number of clusters.

## Definitions and context

The metric space M = (D, d) on a data domain D with the distance function d : D × D → R postulates:

*Non negativity* : ∀*x, y* ∈ *D, d*(*x, y*) ≥ 0 (1a)

*Symmetry* : ∀*x, y* ∈ *D, d*(*x, y*) = *d*(*y, x*) (1b)

*Identity* : ∀*x, y* ∈ *D, x* = *y* ⇔ *d*(*y, x*) = 0 (1c)

*Triangle inequality* : *x, y, z D, d*(*x, z*) ≤ *d*(*x, y*) + *d*(*y, z*) (1d)

The conditions specified above are satisfied by most discrete or continuous distance (or similarity) metrics (or measures): Euclidean, Minkowski, Manhattan, quadratic form distance (i.e., colour histograms, weighted Euclidean distance), edit distance, Jaccard's coefficient or Hausdorff distance. Building clusters of objects in metric spaces relies on the partitioning method and shape of the decision boundary between two adjacent clusters. The partitioning method regards how a set of objects is split into two or more clusters taking into account specific soptimisation criteria such as the sum of squared errors (SSE) in the case of the simple k-means algorithm. Regarding the decision boundary, the two most common options are ball partitioning as in metric spaces and hyperplane partitioning.

The current implementation of the MTree algorithm is based on the two-level ball decomposition sgeneralisation of the approach from [40]. The limitations from [40] regard choosing an arbitrary object as the pivot, using only binary splits around the median object, which implies previously sorting the objects and multilayered approach due to recursive construction. From the practical perspective of running a clustering process, these are substantial limitations because ordering may not always be possible, binary splitting may not be helpful when the dataset consists of many clusters and the notion of the cluster become unclear in a multilayered approach.

**Definition 1.** The newly designed MTree data structure is a two-level perfectly balanced multiway tree that indexes a set of objects into its leaves which reside only on the second level. After building the tree, the root contains the set of centroids and their corresponding covered radius. On the second level, the leaves represent the clusters containing objects whose distance is smaller or equal to the radius assigned of the corresponding centroid within the root.

The key features for the sparametrised MTree implementation are:

* + 1. The possibility to process various object data types provided as input (i.e., image, document, etc.) that is represented as a multidimensional vector.
    2. The possibility to set up a particular distance function between objects by direct usage of distance functions that are already available in Weka or by using a newly defined custom function.
    3. The possibility to set up a particular division policy that will be used internally used as needed. Practically, the logic of the division policy is managed by the clustering algorithm. This feature needs to be accompanied by a parameter that controls the number of clusters into which full leaf may be splitted. Available options are binary object partitioning (BOP), ternary object partitioning (TOP) or multi-object partitioning (POS).
    4. The possibility to set up a specific number of clusters in which the entire dataset will be partitioned, if the number of clusters is known. If the number of clusters is not known, the MTree will find the optimal number of clusters considering the other parameters that have been set
    5. The possibility to compute at request various clustering quality metrics that will give a general idea on the quality of the clustering process. This feature is critical in benchmarking the MTree clustering results against results produced by other clustering algorithms.

The MTree uses only one node data structure for the roots and leaves. In the root node, the instances are represented by centroids, and each element from the radix vector represents the covered radius for the corresponding centroid. In the same way, each element from the route vector is an address of the corresponding leaf node. Their vector position accomplishes the correspondence between centroids from the root node and covered radius and leaves. For example, the first element of the instances vector of the root represents the first centroid with a radius defined in the first element of the radix vector. The first element of the route vector represents the address of the leaf node that contains objects whose distance to the first centroid is smaller or equal to the covered radius. In the case of leaf nodes, the instances represent the data objects themselves. The *isLeaf* flag is set by the business logic to value TRUE such that radix and route vectors are set to null.

Before starting any computation needed for inserting a new object in the MTree, the algorithm checks if we are in a leaf and if the leaf has objects in it. Suppose any of these conditions do not hold, then insertion may not take place because insertion may be performed only in a leaf, and further splitting may be taken into consideration. In that case, insertion may not occur because insertion may be performed only in a leaf, and further splitting may be considered only if the leaf has objects in it. Further, the leaf is evaluated for splitting sparametrised by *evaluatorOfK*, which is a function that determines the optimal number of clusters. This helper function takes as parameter the objects from *treeNode* and outputs *splitEval* as an evaluation of the splitting. If this also is valid, then the leaf node is split into the optimal number of clusters by using a sparametrised *divisionPolicy*. The *insertNonFull* function is called to append a new object in the leaf when no splitting is necessary. The input of *mTreeInsert* function consists of the address for the tree's root and the new object to be inserted in the tree. There is no returned value from this function, and the output is the tree itself with one more object that was added correctly.

The two main ingredients of *mTreeInsert* operation are evaluating the optimal number of clusters from a leaf and the division policy used for splitting. The current implementation uses a function called *voteK* that computes the optimal number of clusters in a similar way as NbClust [6] package in R. The main difference is that NbClust uses 30 indices. At the same time, voteK currently integrates only eight indices: Davies-Bouldin, Dunn, Xi-Beni, Banfeld-Raftery, McClain-Rao, Ray- Turi, Calinski-Harabasz and PBM indices. The architectural design of the package allows the easy call of any method that, given an input dataset, can compute the optimal number of clusters.

Table 1: The structure of MTree node

|  |  |
| --- | --- |
| **Field name** | **Description** |
| nrKeys | The number of objects stored in the node. |
| isLeaf | This flag represents the node type: root or leaf. |
| radixes | the vector of distances covered by a centroid. |
| routes | The vector of node addresses to leaf nodes. |
| instances | the objects from the node (parent or leaf). |
| parent | the address of the parent node. |

The nrKeys represents the number of items (i.e., centroids or items) contained in a node (i.e., root or leaf). For the root node, the items are centroids, and for the leaf node, the items are the sample points. Depending upon the implementation, the centroids may be items from the dataset or computed instances. The isLeaf field from the data structure represents a clarification regarding what represent the items from a node: centroids or instances.

As far as our M-tree is concerned, we pay extra attention to the nodes because it is essential whether they are leaves (i.e., terminal nodes containing instances) or internal nodes (i.e., having only centroids) information is critical for the algorithm design.

The instances vector contains the centroid points or items, depending upon the node is either root or leaf. If the node is the root, vector radixes contain the distance covered by each centroid, while the routes vector contains the leaves' addresses. On the other hand, if the node is a leaf, then the field parent includes the root address while the radixes and routes vectors are empty.

The second key ingredient of the *mTreeInsert* function is the division policy. The default option for this parameter is the simple k-means algorithm, but any other strategy may be called as needed. Other options, besides calling particular clustering algorithms as a multi-object partitioning (MOP) strategy, is using binary space partitioning (BSP) or ternary object partitioning (TOP) by simply setting proper sparametrised values. Suppose there is no need for node splitting, then insertion reduces to appending the new object into that leaf. In that case, insertion reduces to appending the new object into that leaf, which is accomplished by calling *insertNonFull* function. Intuitively, when a leaf is not full, we insert a new object; otherwise, we split the leaf. The most crucial difference from former versions or other approaches is that splitting is not called when the number of stored objects reaches a specific value, but when current objects exhibit the property that they are properly clustered, and therefore a split is compulsory.

Algorithm 1 ssummarises the business logic for inserting a new object into an existing MTree leaf node. The second critical procedure is the one that performs the split of a leaf node as specified in the insertion algorithm. The main ingredient is represented by the *clusteringEvaluator* setup, which allows breaking the leaf into clusters according to with specific division policy and a predetermined optimal number of clusters. The newly obtained clusters are added into a *splitedClusters* vector and returned as output. The main improvement in the split procedure is avoiding splitting a leaf into a hard-coded number of clusters by using a pre-determined optimal number of clusters and sparametrising for the division policy for running the effective split. Algorithm 2 ssummarises the business logic for splitting. The input consists of a tree node (i.e., a cluster) and an evaluator, and the returned value consists of a vector of clusters, called *splittedClusters*. The evaluator has the task of deciding if the node should remain as a single cluster or be split in two or more clusters. If the evaluator considers more than one cluster in the note, the node will split, and the tree will change its structure.

The bounding volumes of the MTree leaf nodes are circles if objects are 2-dimensional or spheres if objects are 3-dimensional, and Euclidean distance is being used. For n-dimensional spaces, the bounding volumes are hyperspheres, a sgeneralisation for a set of points equally distanced to a given point. This sgeneralisation is valid only for Euclidean distance; as for other distances, the bounding volume is the representative of a sphere for that particular vector space.

## MTree algorithms description

The MTree implementation is aimed for usage by client code in practical scenarios. Although the primary usage scenario addresses the situation for which we know the actual number of clusters, the clusterer may also be used in the case when the data analyst specifies a particular number of clusters depending on the tackled task or in the situation when the number of clusters is not known or does not exist.

In any of the situations mentioned above, the parameters that need to be set are the input dataset, the number of clusters, the distance metric, the evaluator of the number of clusters and the division policy algorithm. The main practical goal of the current version of the MTree clusterer is to verify that it correctly loads the data given specific parameters and creates a data model that validates the ground-truth model from two publicly available data sets. Finally, the clustering validation metrics are verified against other clustering algorithms implemented in Weka workbench.

One key aspect for correctly building the MTree from data regards the order in which the data objects are provided as input. As a general rule, any clustering algorithm is highly sensitive to the order in which data objects are considered in the clustering process. The seed mechanism is the general solution to clustering algorithms and is also used as a standard option in the MTree. For our case, the seed mechanism represents a random shuffle of the order in which the instances are added to the MTree.

The pseudocode of mTreeInsert function presents the structure and logic of operations when inserting a new instance into the tree. The function's parameters are the address of the tree and the item that should be inserted. Since inserting takes place only in leaf nodes, the algorithm first checks that we are in a leaf node and then determines the optimal number of clusters from that leaf. If more than one cluster is found in the leaf, the node is split, and the instance is placed into the appropriate cluster.

**Algorithm 1** mTreeInsert (MTree treeNode, Instance newObject)

1: **if** *treeNode* is leaf and has objects **then**

2: **Set** clusteringEvaluator = getOptimalNrOfClusters (treeNode, *evaluatorOfK*);

3: **end if**

4: **if** *splitEval* is valid **then**

5: nrOfClusters = clusterEval.getNumberOfClusters ();

6: **if** *nrO f Clusters >* 1 **then**

7: splitNode(treeNode, clusteringEvaluator);

8: **else**

9: insertNonFull(treeNode, newObject);

10: **end if**

11: **end if**

**Algorithm 2** mTreeSplitNode (MTree treeNode, ClusterEvaluation clusteringEvaluator)

1: clusters = getClusters (treeNode, clusteringEvaluator);

2: **if** size of clusters *>* 1 **then**

3: **for each** cluster **in** clusters **do**

4: centroidInstance = chooseCenter(cluster);

5: splitedCluster.addCentroid(centroidInstance.getCentroid());

6: splitedCluster.setRadix(centroidInstance.getRadix());

7: splitedClusters.add(splitedCluster);

8: **end for**

9: **end if**

10: Return splitedClusters;

The pseudocode of mTreeSplitNode function actually performs the split of a leaf. Along the treeNode, an evaluator is given as parameter, which gathers the parameters needed to determine the clusters. Once the clusters are determined, the centroids and corresponding radixes are placed in the root, the addresses of the new clusters are placed in the routes and instances themselves are placed in the appropriate clusters.

A particular situation occurs when we do not know the correct number of clusters. In this case, the adequate solution is to preprocess the dataset to check clusterability and determine the valid number of clusters if such a number exists. The situation in which the dataset has not a well-defined structure may be interpreted in two ways: either the dataset has several possible options as the actual number of clusters, or we do not know the correct number of clusters. In the first situation, a domain knowledge person should consider the specific data analysis task and choose the correct number of clusters that fit the practical problem. More extensive work needs to be done as a preprocessing step in the latter situation.

As a general rule, when the dataset has no structure, the first preprocessing steps should define the number of clusters as a task-dependent value. Then, the centroids should also be defined as representatives for each cluster considered by the domain knowledge person. Finally, the objects from the dataset are added to the pertaining cluster only if a maximal threshold distance from the centroid is not exceeded. The objects that have almost equal distance from centroids are considered outliers and are not added to any cluster. In this way, the data analyst may obtain a clusterable data set with a specific number of clusters. Having a clusterable dataset is a prerequisite for the MTree clustering algorithm and any other algorithm. Therefore, if the dataset does not meet clusterability, building an MTree clusterer or any other clusterer will exhibit undefined behaviour.

Finding the correct number of clusters by using MTree may be performed by running with various parameter settings in terms of the number of clusters and division policy in an attempt to obtain a clusterer whose validation parameters show that the correct patterns have been discovered. In this use case, the MTree data structure is built for finding whatever clusters are to be found.

A picture containing text

Description automatically generated

Figure. 1. The internal structure of the root node

Diagram

Description automatically generated

Figure. 2. Sample MTree

Diagram

Description automatically generated

Figure. 3. Sample MTree split node

## Complexity analysis

The complexity analysis of building the MTree from data depends on the number of objects, the number of clusters, the method of finding the optimal number of clusters and the number of distance computations. The number of clusters from the dataset represents the number of splits that need to be performed while building the tree. The most critical operation is finding the optimal number of clusters, which is called after each object insertion. The number of distance computations is related to the number of clusters since distances from the newly inserted object to all the centroids from the root need to be computed to determine the suitable leaf where the insertion should occur. The most time-consuming function is the *getOptimalNrOfClusters* function that is called whenever a new object is to be inserted. We have observed that for a reasonably small number of clusters and a large number of objects, that method getOptimalNrOfClusters is used to trigger a split fewer times than the number of clusters. For example, once the number of leaves from MTree has reached the true number of clusters, then looking for the optimal number of clusters becomes useless. Further insertions will be performed in constant time just by determining the proper leaf where the new object needs to be inserted. As stated in [15], the performance of building an MTree with n objects is analogous to that of k-d trees, that is O(n log n) for the worst-case scenario. Depending on the split method, the time may increase to O(n log 2n) or O(kn log n) for k dimensions. Still, the currently proposed method is highly sensitive to the order in which objects are being inserted, the seed selection and the particular parameters set up, as well as all other clustering algorithms.

The critical property of the MTree is that after correctly building the clusters, the operations of inserting, removing and querying may be performed in O(log n) time. Current works do not test these aspects and need to be further experimentally investigated in practical clustering tasks.

# Experimental results

## Data-sets description

Experimental results have been performed on two synthetic publicly available data sets from the clustering basic benchmark [19]: Unbalance [35] and Dim2 [28]. Unbalance is a synthetic 2-d dataset with 6500 points and 8 Gaussian clusters for which ground truth centroids and partitions are known. Dim2 is also a synthetic 2-d dataset with 1351 points and 9 Gaussian clusters. Figures 4 and 5 present a plot of the raw input data.

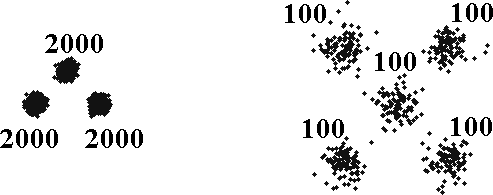


Figure 4: Unbalance dataset



Figure 5: Dim2 dataset

We have chosen two synthetic data sets for which the ground truth centroids and partitions are known because they are suitable for comparing clustering results obtained by MTree algorithm against other ones implemented in the Weka workbench.

Finally, we have tested the MTree on Wine and Iris classical datasets from UCI Machine Learning Repository [3]. These real-world data sets were chosen because they may be successfully used in clustering tasks as they are labelled, and classical unsupervised training may correctly determine the classes.

## MTree package description

MTree is implemented in Java and aims to be executed within Weka 3.8 workbench using the Package manager tool. The MTree package is based on Node, MTreeBean and MTree classes, and the other three helper classes. Figure 6 shows the software architecture of the MTree package as a UML class diagram.

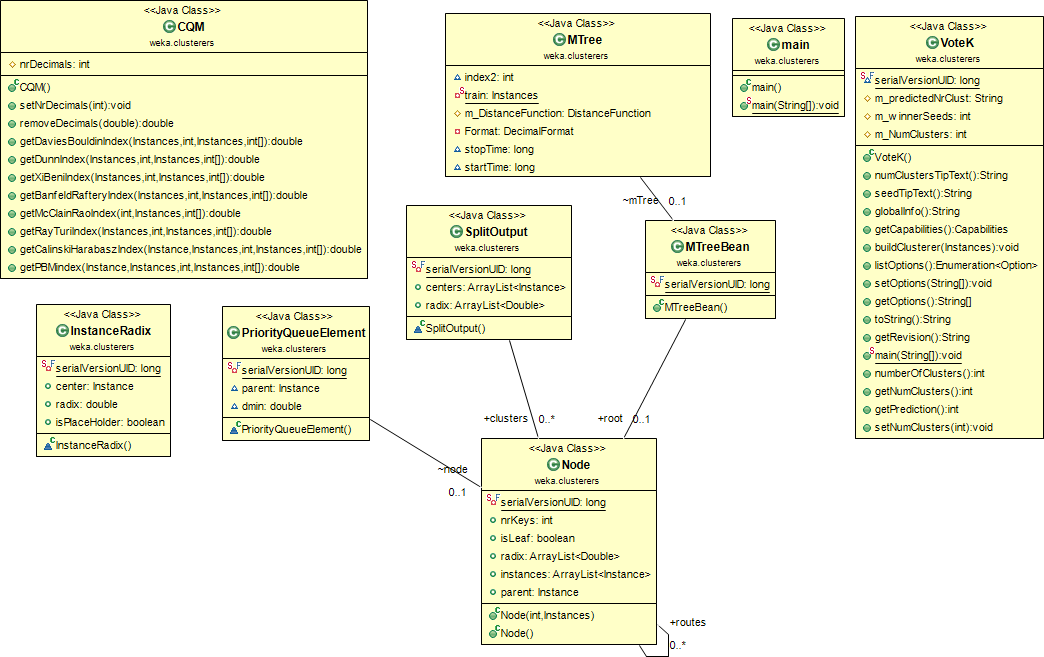


Figure 6: UML class diagram for MTree package

The class Node represents a blueprint for a cluster of instances, and the MTreeBean class contains the root of the MTree. The most important class is MTree, which extends RandomizableClusterer, which is an abstract class whose direct subclasses are Canopy, Cobweb, FarthestFirst and SimpleKMeans classes. Further, by implementing the NumberOfClustersRequestable and other interfaces, the MTree gets the possibility to be sparametrised similarly as different clustering algorithms are in Weka.

The main goal was to obtain a clusterer that may be sparameterisable in the same way as already existing clusterers based on interfaces already defined in Weka but also offering the possibility of defining new interfaces specific for parameters needed by MTree algorithm. In this way, the newly obtained MTree can be easily sparametrised by using the command-line interface or Weka GUI interface.

## Sample MTree usage

The MTree can be used in three ways. The current implementation provides flexibility for running full experimental runs and benchmarking the performance of an MTree parameter configuration against already existing Weka clustering algorithms.

* *Basic mode, through the command line*. This mode allows executing the MTree on any machine that has JVM 1.8 and *weka.jar* version 3.8.3. Figure 7 presents a sample command line execution of the MTree algorithm. This approach is commonly used when batch execution is needed only once for building the clusters and sserialising the obtained model (i.e., the distribution of objects into clusters) to persistent storage (i.e., csv, xml, etc.) for later usage is rather tricky.

The available options when running MTree in the command-line interface are further presented. ***N*** represents the number of clusters. If we want MTree to decide for itself the number of clusters this option must be set to value -1. ***init*** option may be used for setting the sinitialisation method. ***I*** option is for setting the maximum number of iterations, ***O*** for preserving the order of instances, ***S*** for setting the number of seeds, ***d*** for setting the distance metric, ***findN*** for setting the method for finding the optimal number of clusters and ***splitPolicy*** for setting the method used as splitting policy. The current implementation may use as splitting policy Canopy, Simple k-means, CobWeb, FarthestFirst or HierarchicalClusterer clusterers from Weka.

Figure 7: Command line execution of MTree



* *Using the Weka GUI*. This mode is the most user friendly as the MTree may be used from Weka GUI as any other clustering algorithm. As the MTree package is in the list of official packages, it needs to be installed before usage. Installing the MTree package in Weka is a straightforward procedure as the *MTree.zip* archive is publicly available in SourceForge [30]. The link to the package is available in the list of official packages within the Weka package manager tool.
* *Programmatic way*. The most versatile usage of the MTree is programmatic. This approach allows setting up the parameters at runtime and having a ready-to-use in memory MTree object that is ready for querying. This approach enables the usage of the cluster as business logic on a server-side in complex applications where client code is performing various queries. Sample code for building the MTree from data is publicly available in [8].

## Sample runs on Unbalance and Dim2 synthetic datasets

The newly released sparametrised MTree implementation has been tested against two publicly available synthetic data sets: *Unbalance* and *Dim2*. The client code that calls the MTree package is publicly available at [8]. As further presented, experimental results were obtained by programmatically running the MTree implementation.

Figures 9 and 10 present the experimental results of running the MTree clusters along the other five clusterers implemented in Weka workbench: Canopy, EM (expectation-maximisation), FF (Farthest First), HC (Hierarchical Clustering) and SKM (Simple KMeans).

As Figure 9 clearly shows, the MTree correctly determines the clusters by using 100 seeds and Canopy for split policy. As a general rule, the clustering result exhibits undefined behaviour regarding the number of seeds. Correct results may be obtained sometimes for only ten seeds and sometimes for 1000 seeds. Here is a summary of the experimental results of the other five algorithms:

* *Canopy* algorithm fails to determine the correct number of clusters, and the found distribution into clusters is wrong.
* *EM* algorithm fails to determine the correct number of clusters. However, it is used for this task in many situations as it does not require the value of K. The obtained clusters are reasonable fine with two exceptions: cluster 0 puts together three real clusters, and cluster 1 puts together two real clusters.
* *FF* algorithm correctly determines the number of clusters but misses to determine two of them correctly: cluster 0 puts together two real clusters, and cluster 2 is composed of objects belonging to two distinct clusters.
* *HC* algorithm correctly solves the task.
* *SKM* algorithm correctly solves the task after finetuning the parameters: 100 seeds, usage of kmeans++ [2] for seed soptimisation and maximum 10,000 iterations.

As Figure 10 clearly shows, the MTree correctly determines the clusters on a more difficult task by using only ten seeds. The other investigated algorithms provide the following results:

* *Canopy* algorithm fails to determine the correct number of clusters, and the found distribution into clusters is wrong, as it puts together objects from two clusters in a cluster.
* *EM* algorithm correctly determines the clusters.
* *FF* algorithm fails to determine the correct number of clusters and misses to choose one of them correctly. The result shows that objects from one real cluster are split between two real clusters.
* *HC* fails to determine the correct number of clusters and reports one found cluster joining two real clusters.
* *SKM* algorithm correctly solves the task after fine-tuning the parameters: 10 seeds, usage of kmeans++ [2] for seed soptimisation and maximum 10,000 iterations.

Although experiments were performed by programmatically running the algorithms, the MTree package maybe also run using the Weka GUI. Figure 8 presents a sample run of the MTree algorithm with Canopy set as split policy, eight clusters and only one seed.

Figure 8: Execution of MTree in Weka GUI

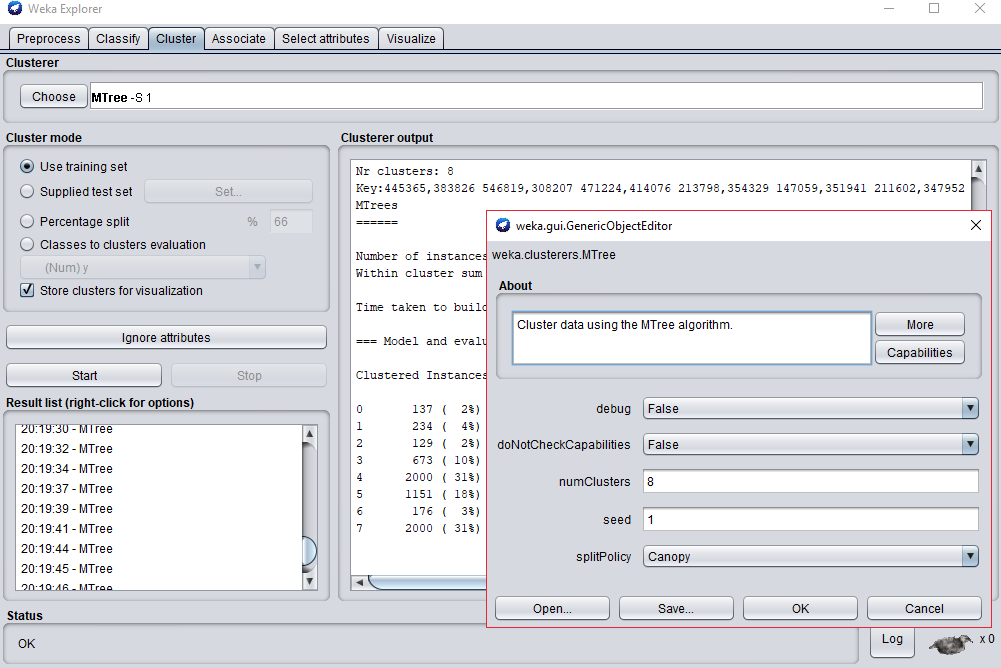
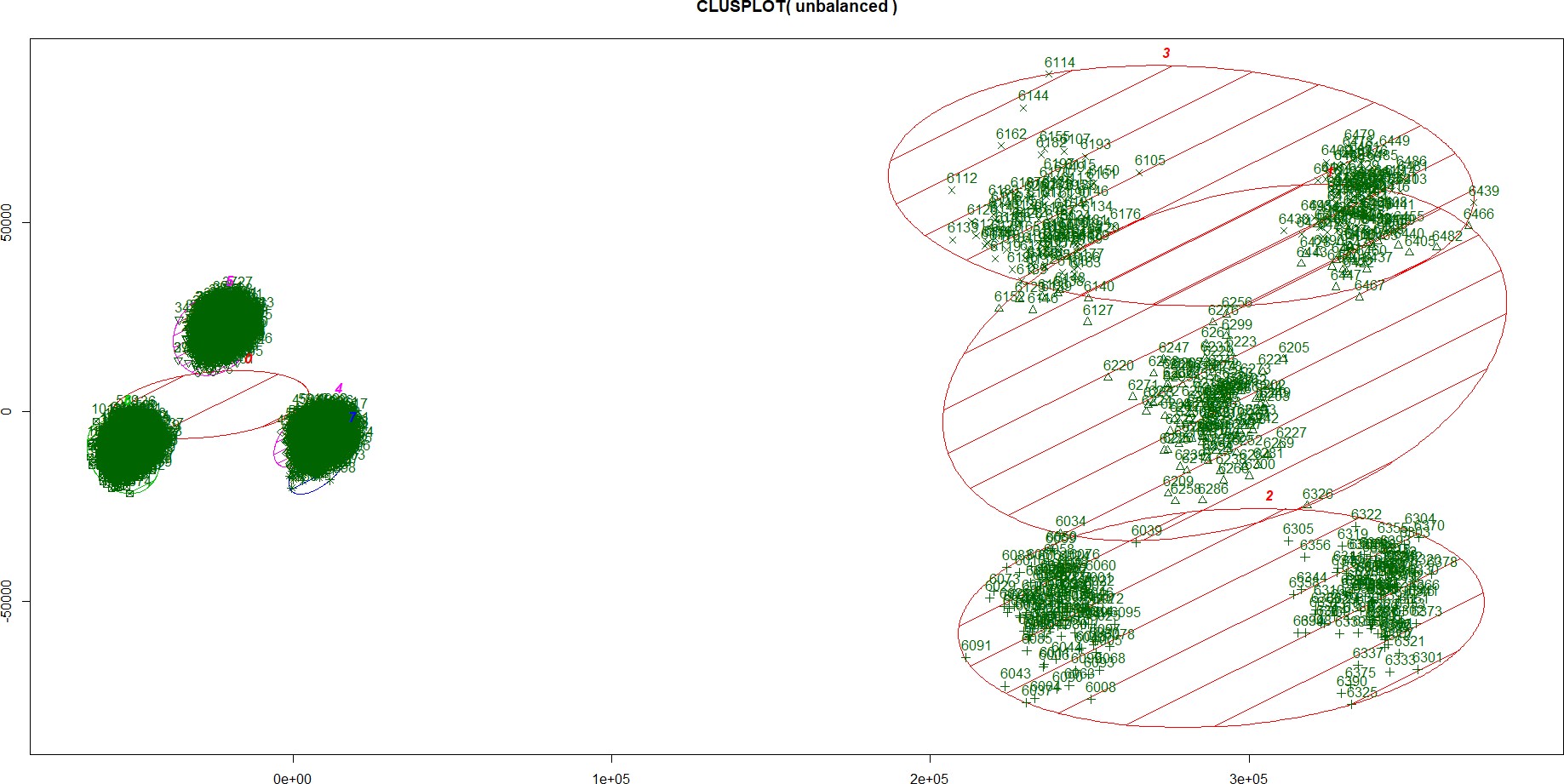


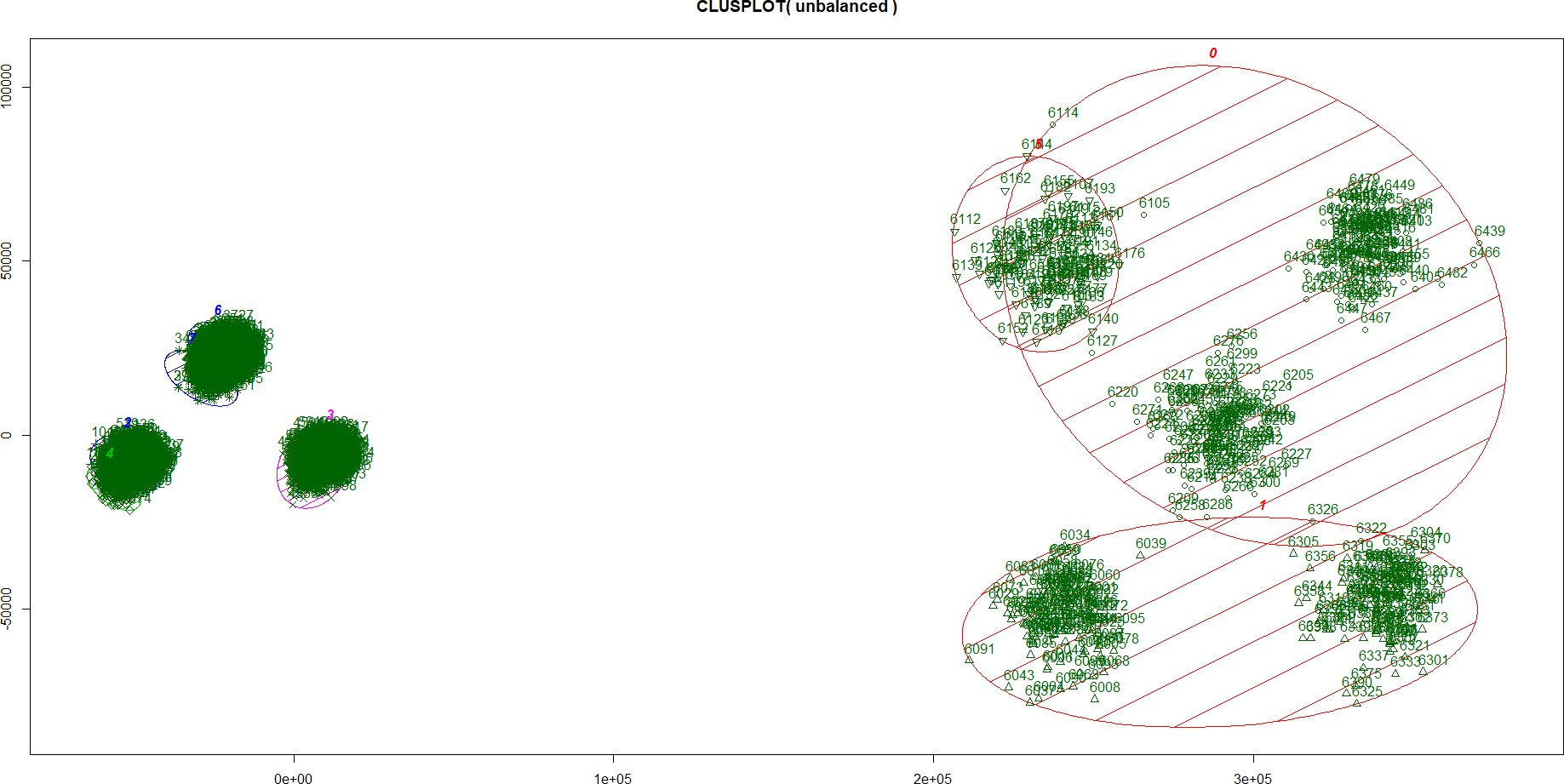
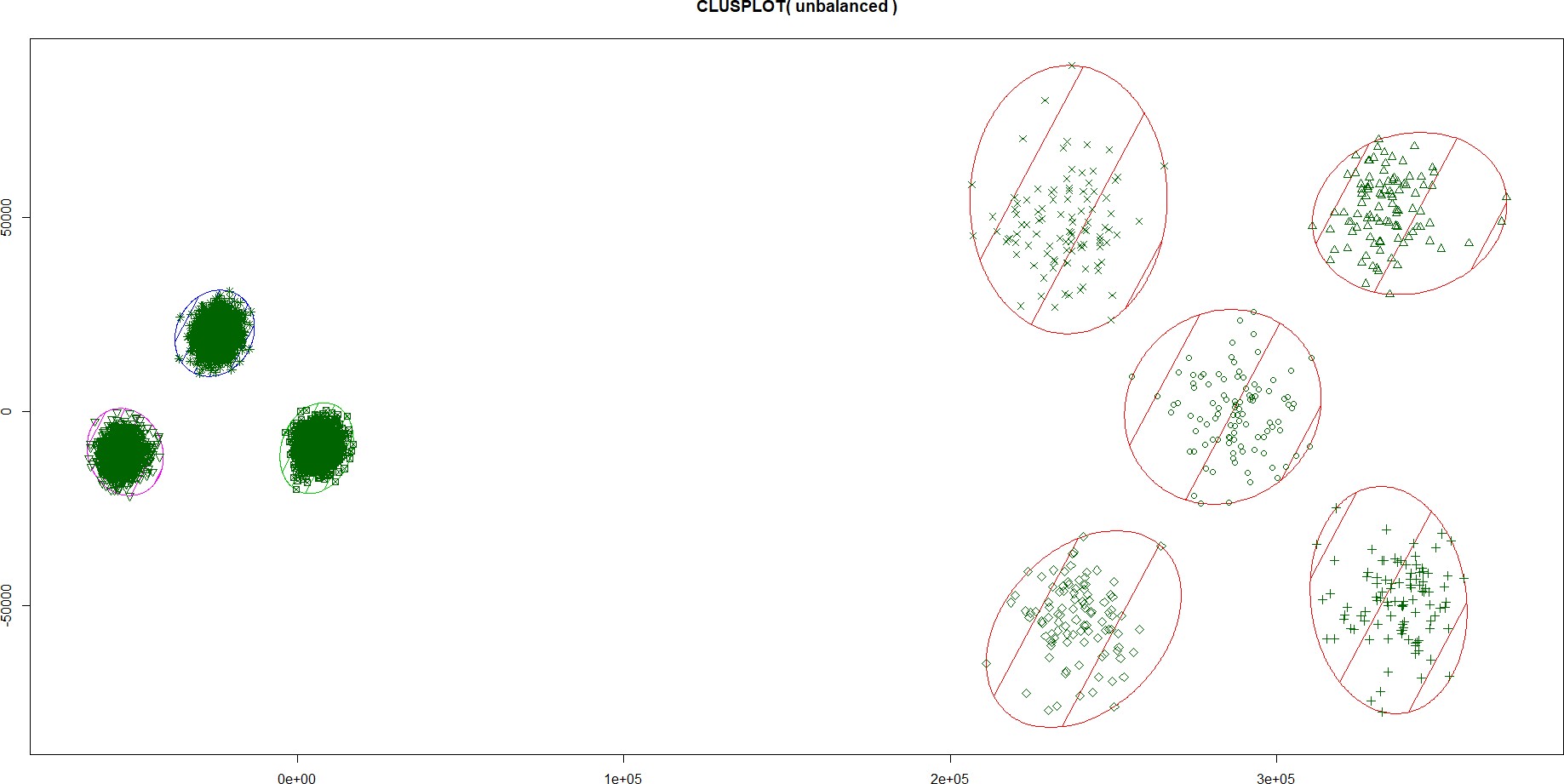
Table 2: Running times statistics (measured in seconds)

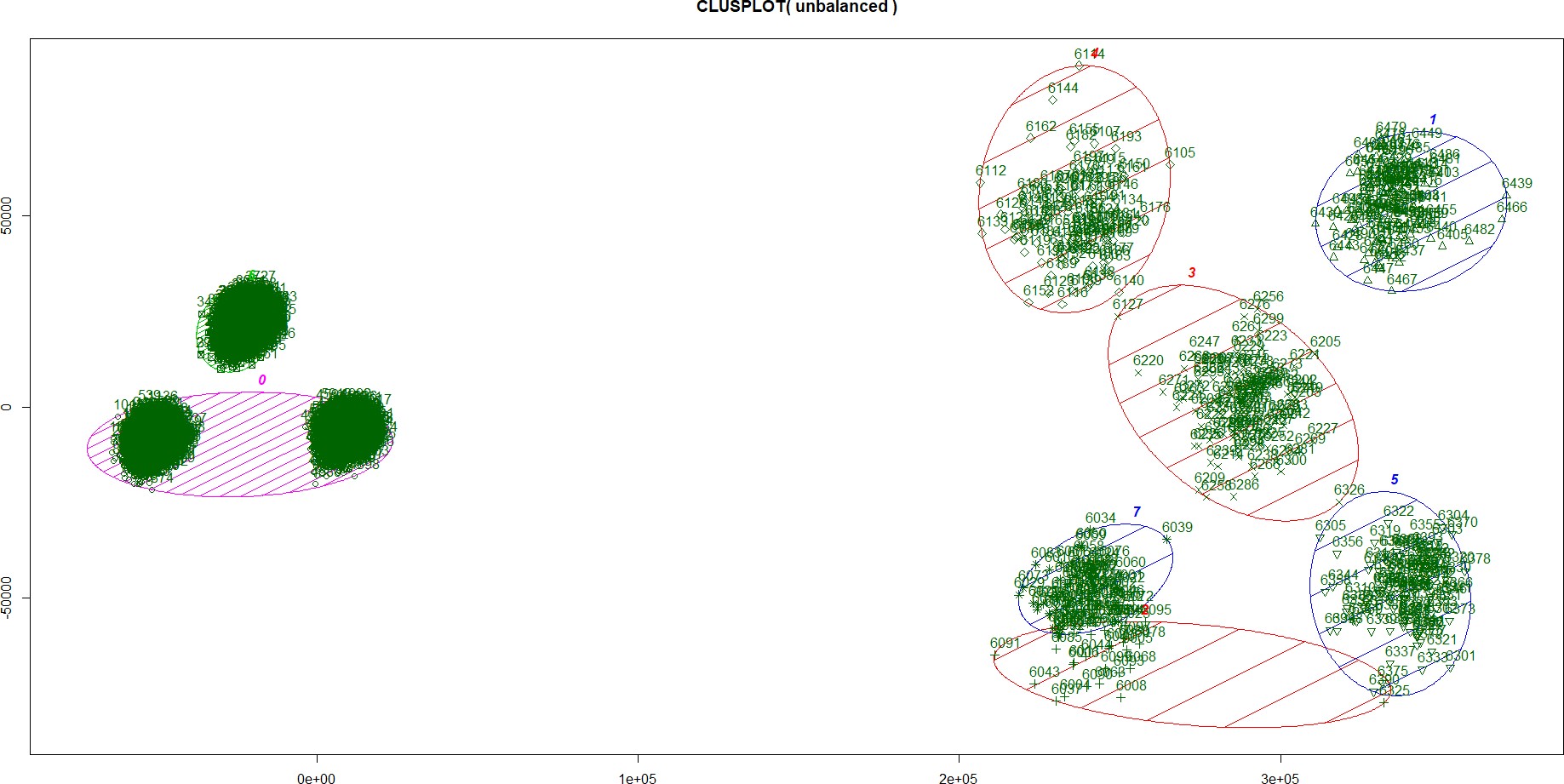
|  |  |  |
| --- | --- | --- |
| **Algorithm** | **Unbalance data-set** | **Dim2 data-set** |
| MTree | 0.3 [per seed] | 0.06 [per seed] |
| Canopy | 0.01 | 0.1 |
| EM | 8.21 [per tuned seed] | 0.55 [per tuned seed] |
| FF | 0.01 [per seed] | 0.01 [per seed] |
| HC | 605.42 | 4.11 |
| SKM | 0.06 [per seed] | 0.01 [per seed] |

Table 3: Performance results on real-world datasets

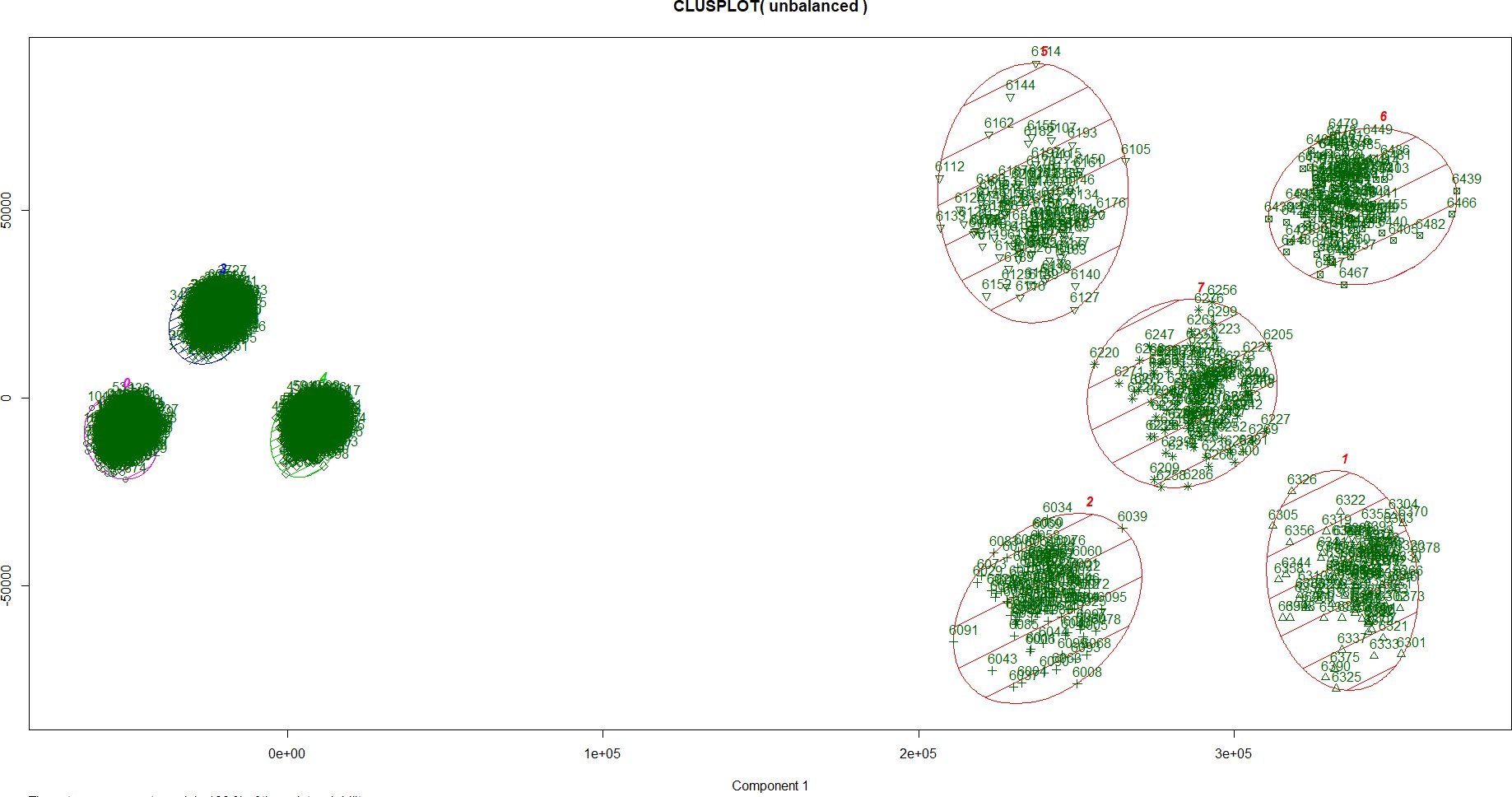
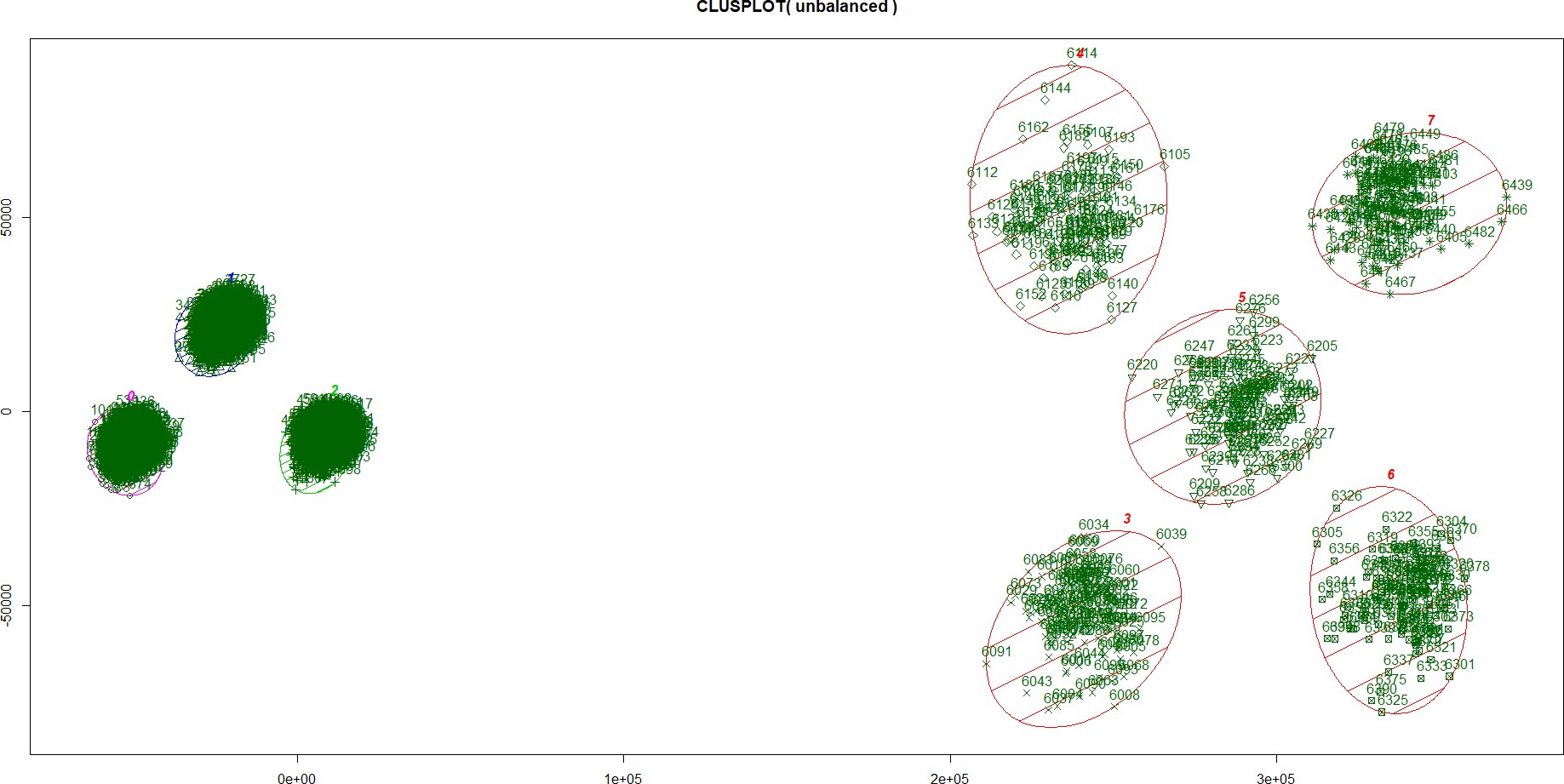
|  |  |  |
| --- | --- | --- |
| **Algorithm** | **Accuracy Wine** | **Accuracy Iris** |
| MTree+Canopy | 0.94382 | 0.89261 |
| MTree+cKMs | 0.92134 | 0.89261 |
| MTree+FF | 0.93258 | 0.88590 |
| MTree+HC | 0.89887 | 0.89261 |
| KMeans | 0.93258 | 0.88590 |



(a) MTree results (b) Canopy results

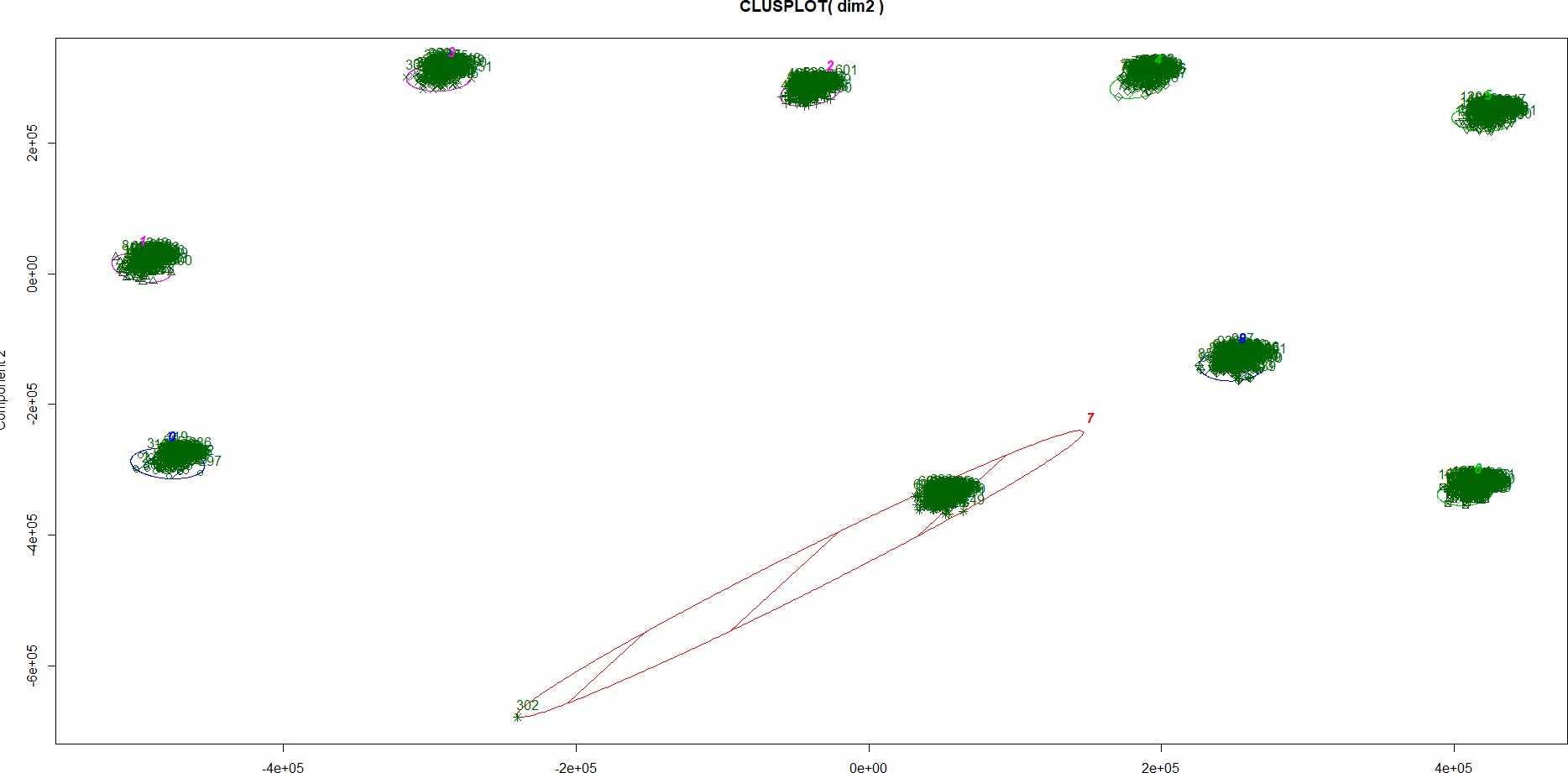
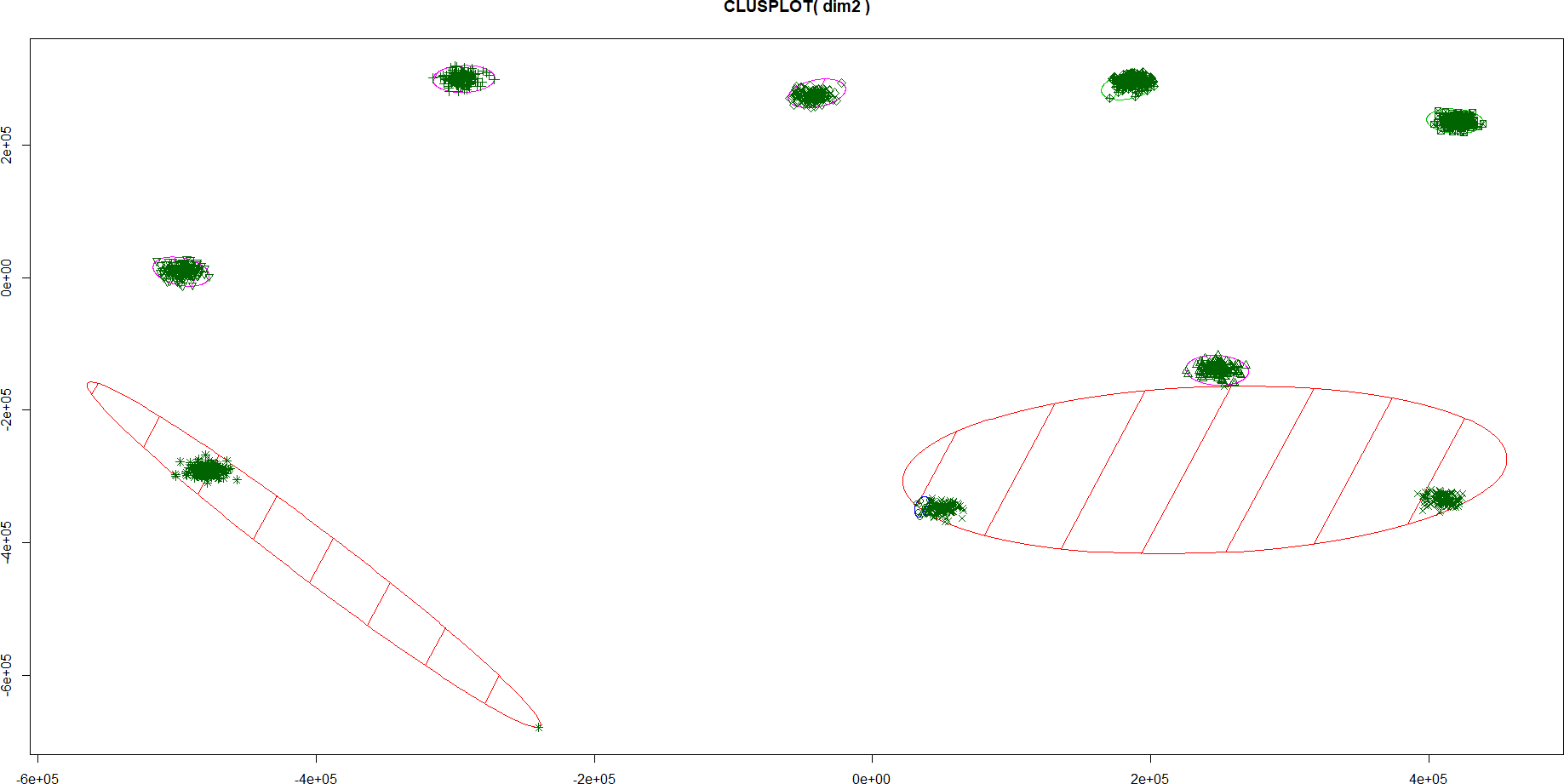


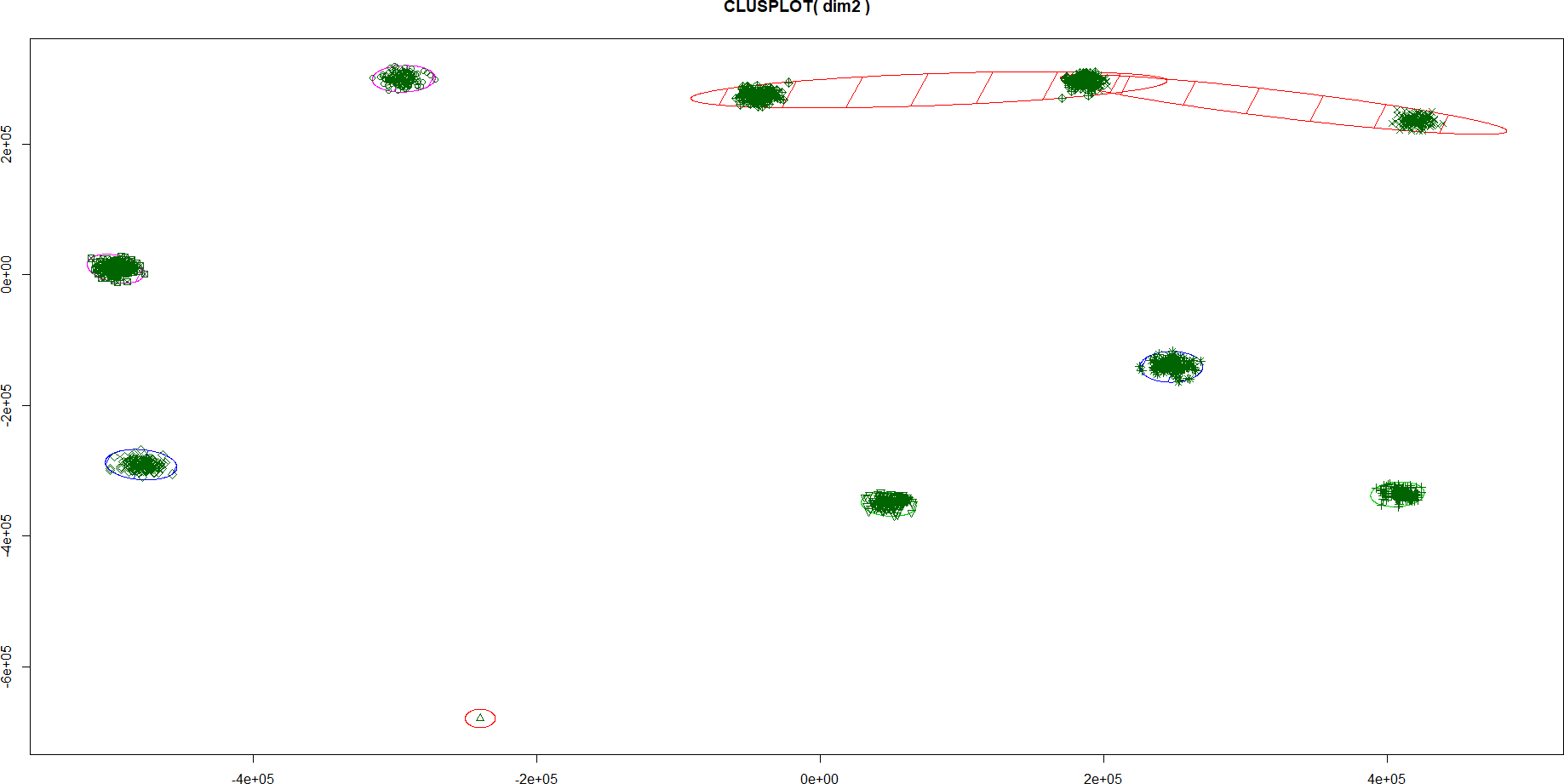
(c) EM results (d) FF results

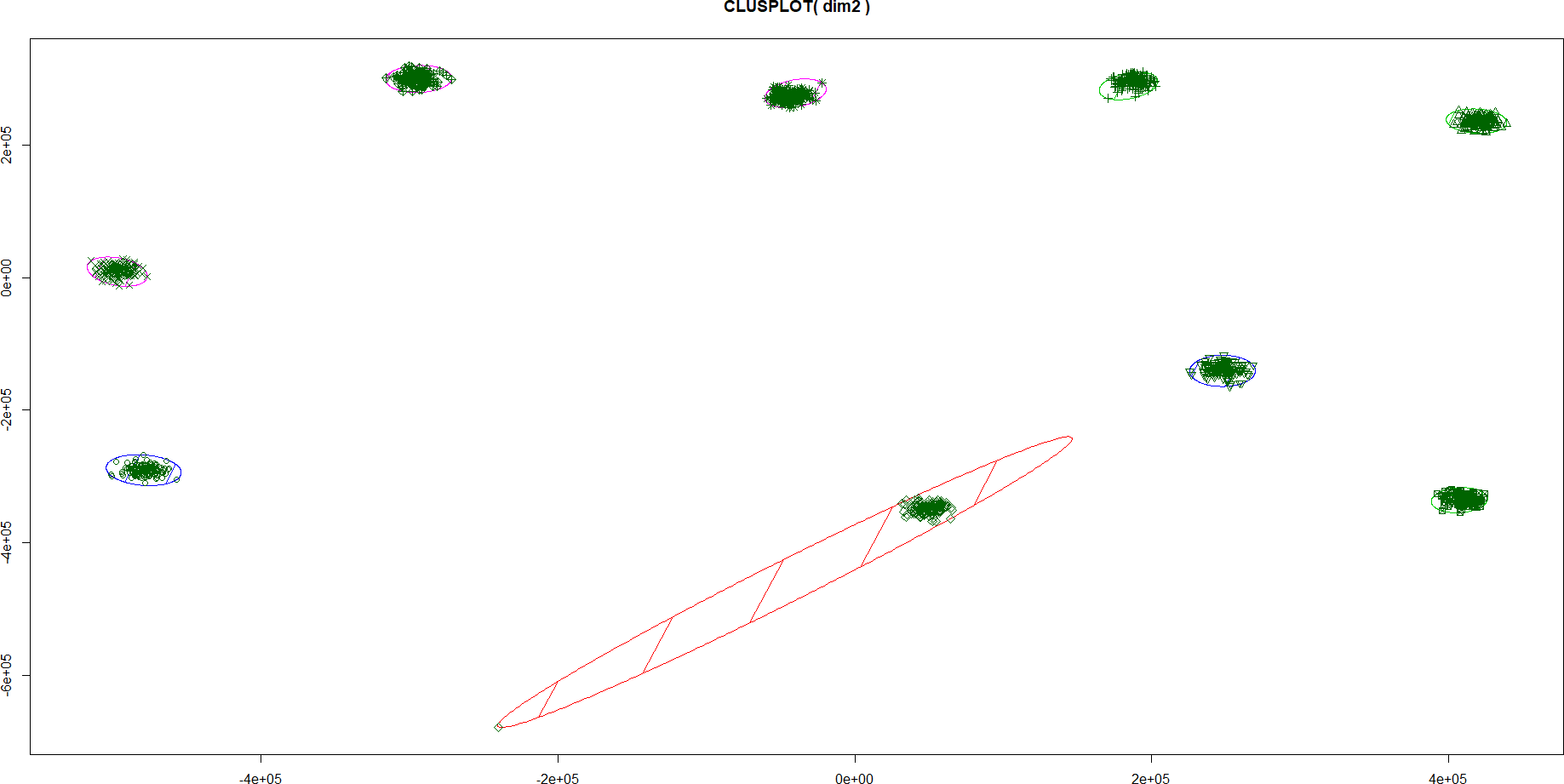


(e) HC results (f) SKM results

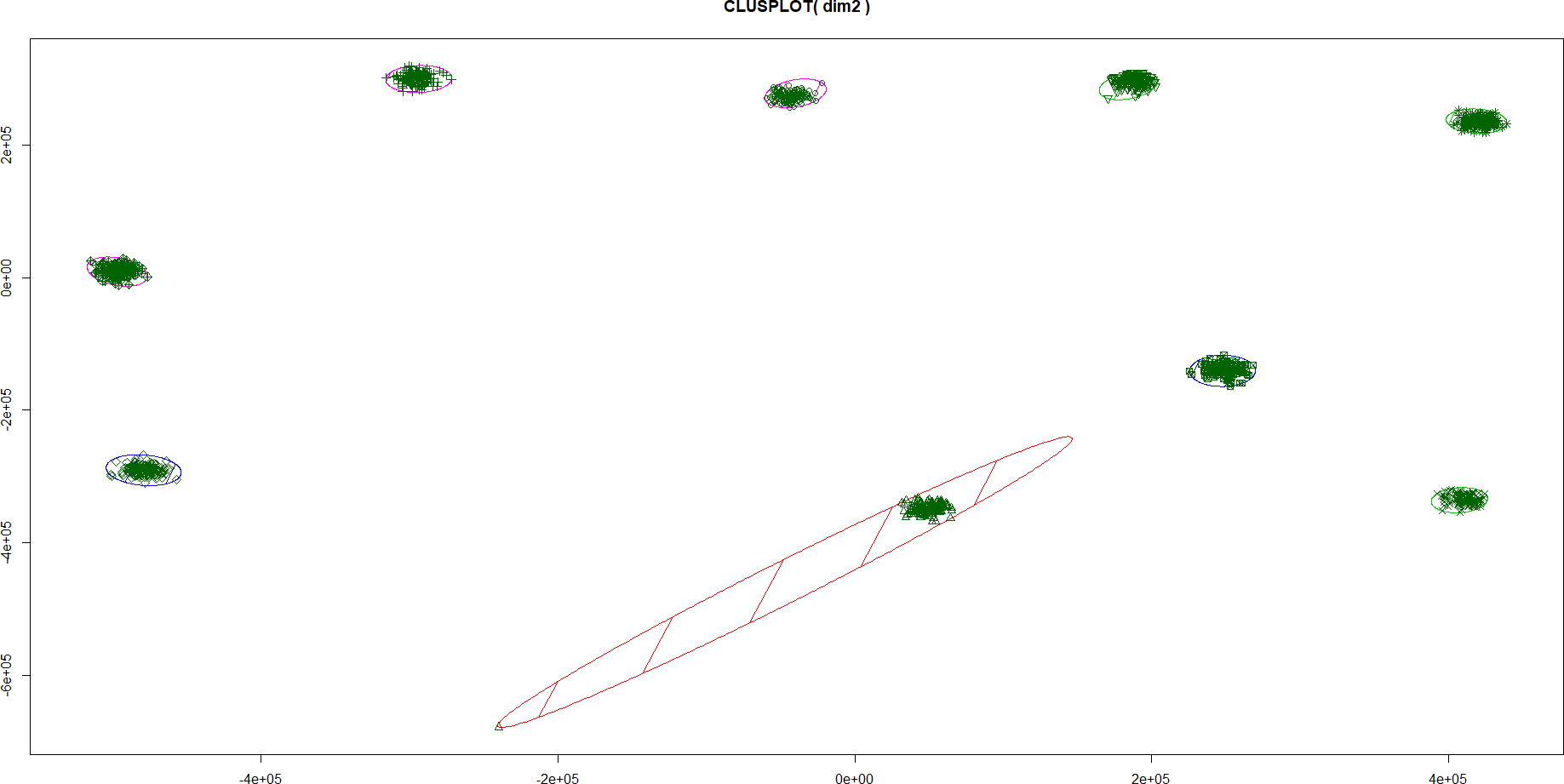
Figure 9: Clustering results on *Unbalance* dataset

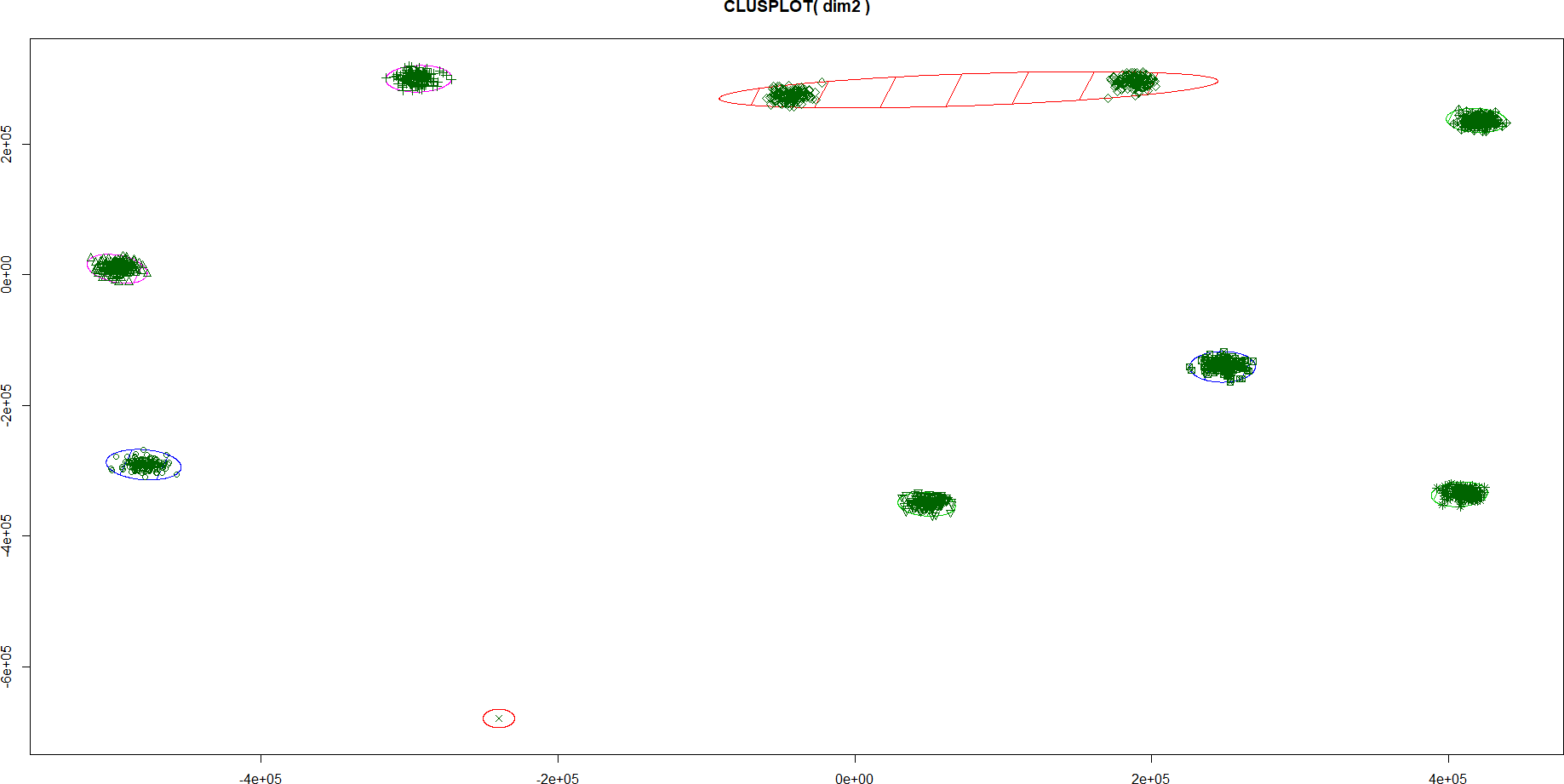
(a) MTree results (b) Canopy results



(c) EM results (d) FF results



(e) HC results (f) SKM results

Figure 10: Clustering results on *Dim2* dataset

Experimental results show that the first K instances have the most significant impact over the final result, where K is the number of clusters. Thus, the current implementation uses kmeans++ [2] seed optimisation, so the first K instances that are added to the MTree are a relatively sparse one from another.

Table 2 ssummarises the running time statistics for all six algorithms on both data sets. In the EM algorithm, each tuned seed has been obtained by more iterations and more k-means runs, a fact that explains the more significant running time. HC and Canopy do not have seeds, and Canopy's poor results on both datasets were obtained regardless of the configuration parameters. The number of seeds for the algorithms that correctly solved the dim2 dataset has been set to 10.

Finally, the SSE (sum of squared error) and the assignment of objects are correctly computed for MTree as they compute the same values as SKM of 4.2471 and 0.3367 for unbalance dim2 datasets, respectively. Therefore, the clusters produced by the MTree are valid and represent the real ones from the data sets, and SSE represents a good soptimisation metric for these data sets.

## Sample runs on Iris and Wine real-world datasets

Wine data were normalised, and then MTree was used on all 13 features. The algorithm was run on 100 seeds, and the best result was targeting to be with the best (smallest) SSE. As smaller SSE does not always provide the best accuracy, we observe that different cluster quality metrics may improve the performance of the proposed algorithm. KMeans run on 100 seeds obtains 93% accuracy or 12 wrong predictions.

Iris data were normalised, and MTree was used on all four features. As on the previous dataset, the algorithm was run on 100 seeds, and best SSE was targeted. It is interesting to notice that different SSE provide the same accuracy; it seems that the algorithm converged with 16 wrong predictions being its best. MTree+cobweb is not able to cluster the data. On the same data, KMeans run on 100 seeds obtains 88% accuracy or 17 wrong predictions.

Table 3 presents accuracy results of MTree sparametrised by various splitting algorithms (i.e., Canopy, KMeans, Farthest First and Hierarchical clustering) against baseline KMeans algorithm. Experimental results show the MTree clustering algorithm correctly finds groups at least as good as the simple KMeans algorithm.

# Conclusions and future work

This paper presents improved sparametrised MTree clusters for Weka workbench. The experimental results show that MTree correctly solves two synthetic data sets for which the correct structure (i.e., number of clusters, centroids and distribution) is known. More, five other clustering algorithms implemented in Weka are outperformed in various situations e because they do not solve the clustering task correctly or need intensive tuning for solving it.

Still, the current approach is used only for *sanity check* of the clustering capabilities of the MTree implementation, rather than solving a particular clustering task on a real data set. The implementation is Java-based and is available as open-source Weka package. The experimental results are correct and promising such that further development under Weka offers the possibility of proper benchmarking of further clustering tasks that may be taken into consideration.

The main contributions are ssummarised as follows:

1. An updated sparametrised version of the MTree package is presented. The parametrisation mainly regards used distance metric, the method for finding and setting the number of clusters and the division policy. After being adequately processed, the data structure can load various object types and provide validation insights.
2. The proposed software architecture of the MTree enables parameterisation through easy integration of other internal algorithmic strategies that perform critical tasks within the business logic.
3. The implementation of the MTreeis available as an open-source package in Weka workbench. This approach allows further usage and benchmarking against other clustering algorithms.
4. The experiments demonstrate that the proposed approach outperforms current clustering algorithms on two datasets.

Future works may take into consideration extending the *voteK* algorithm as a Java implementation of the already existing R package NbClust. Further developing *voteK* should take into consideration the available clustering quality indices and parametrisation capabilities. MTree may try different approaches regarding how objects are processed when building the tree in terms of internal business logic. One option is to cluster the outlier objects later in the process.

As the most expensive operations are finding the optimal number of clusters and splitting, one option is trying to predict how the insertion of an object will impact the tree in terms of triggering a split. Checking for the optimal number of clusters should be performed only when an insert is highly to determine a split, as most inserts do not require a split, especially when the dataset has a well-defined structure.

MTree currently implements range query and kNN query. These implementations should be further tested in practical real data scenarios. Other tasks in which MTree may also be used are outlier detection and finding the correct number of clusters in a data set. Finally, the MTree algorithm may be further tested to find patterns in data when internal structure is not known.

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